



**Utrecht  
University**



This publication is part of the  
project NextGenOpt (with  
project number ESI.2019.008,  
which is (partly) financed by the  
Dutch Research Council (NWO).

ENERGY SYSTEM OPTIMIZATION WORKSHOP

27 Nov 2025

# *Error-free model reduction with low-resolution precursor surrogates*

**Zhi Gao**

PhD candidate at Copernicus Institute of Sustainable Development,  
Utrecht University  
[z.gao1@uu.nl](mailto:z.gao1@uu.nl)

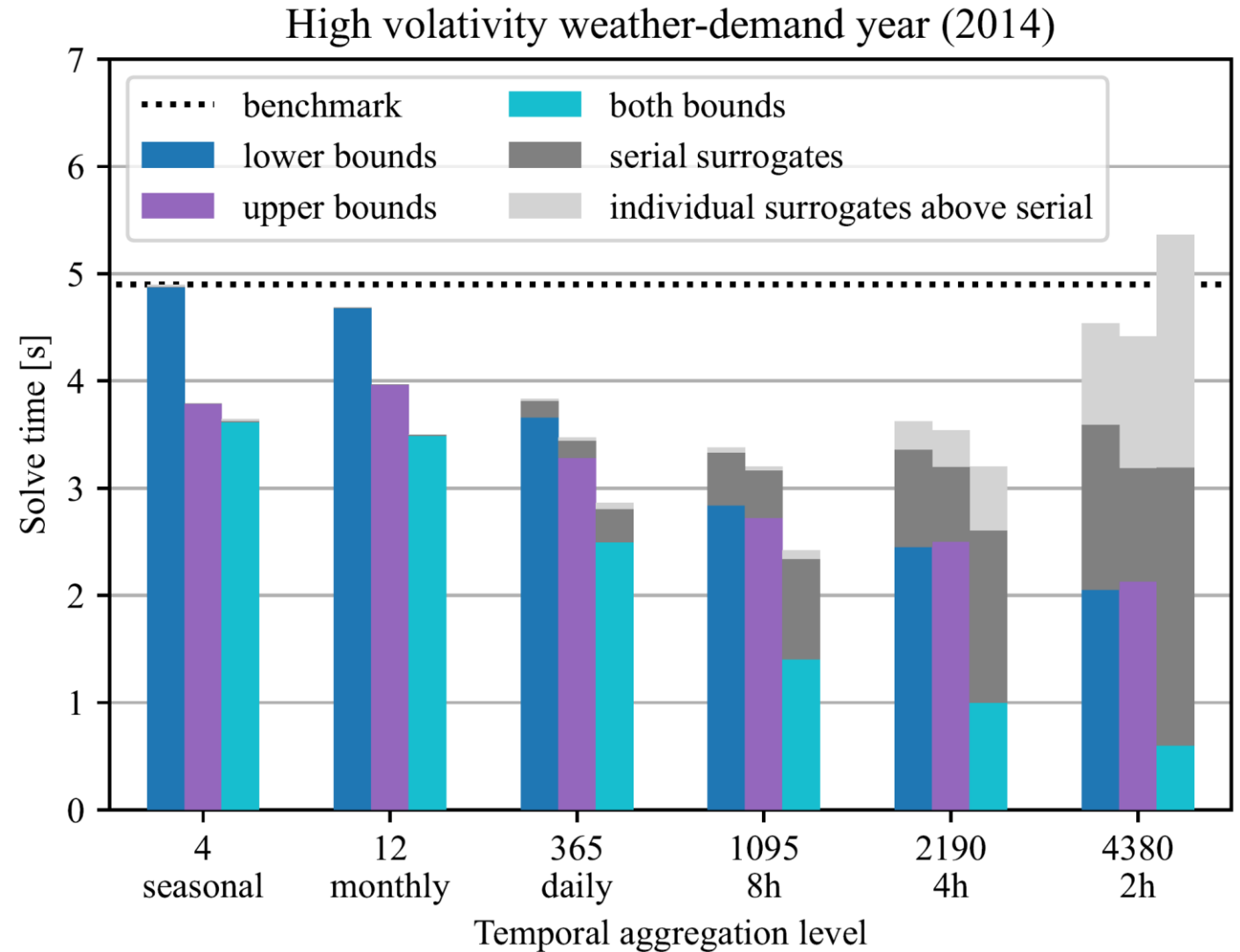


# Overcoming the efficiency-accuracy trade-off

- There are “free lunches”, big lunches
- Why this is ground-breaking
- How, in short
- More on the way

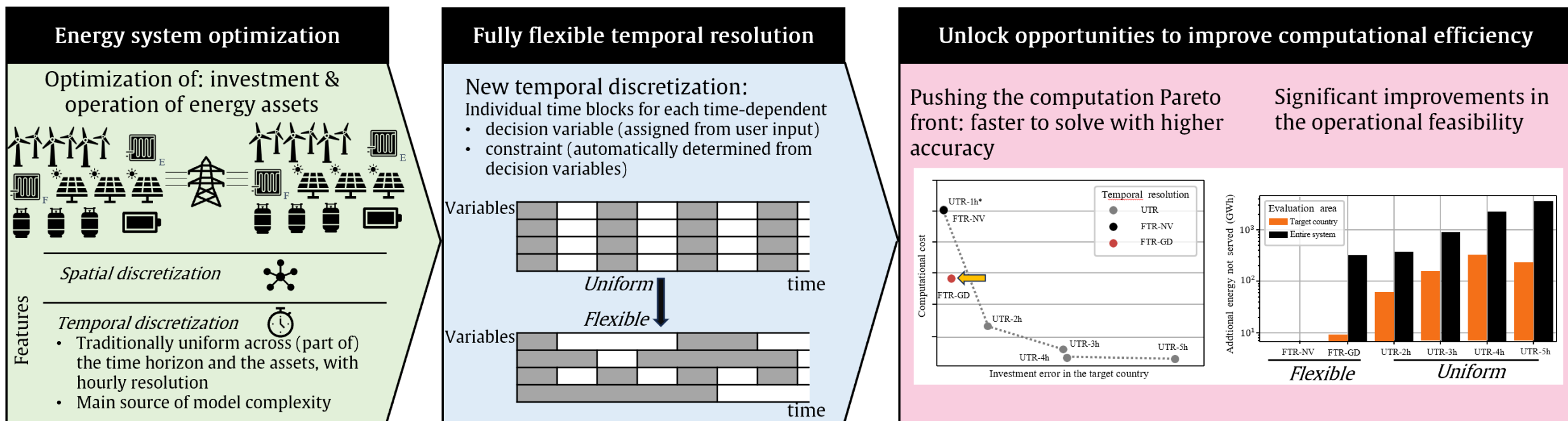
# Free, big lunch

- 100% accuracy,  
no modeling error.
- Solve time down by  
52%
- or 2.13x speedup



# Model reduction comes at the expense of accuracy:

## Most of the time, also shown in our previous work.



[1] Zhi Gao, Matteo Gazzani, Diego A. Tejada-Arango, Abel Soares Siqueira, Ni Wang, Madeleine Gibescu, Germán Morales-España, Fully flexible temporal resolution for energy system optimization, Applied Energy, Volume 396, 2025, 126267, ISSN 0306-2619, <https://doi.org/10.1016/j.apenergy.2025.126267> .

# Model reduction comes at the expense of accuracy: Most of the time, and also shown in our previous work.

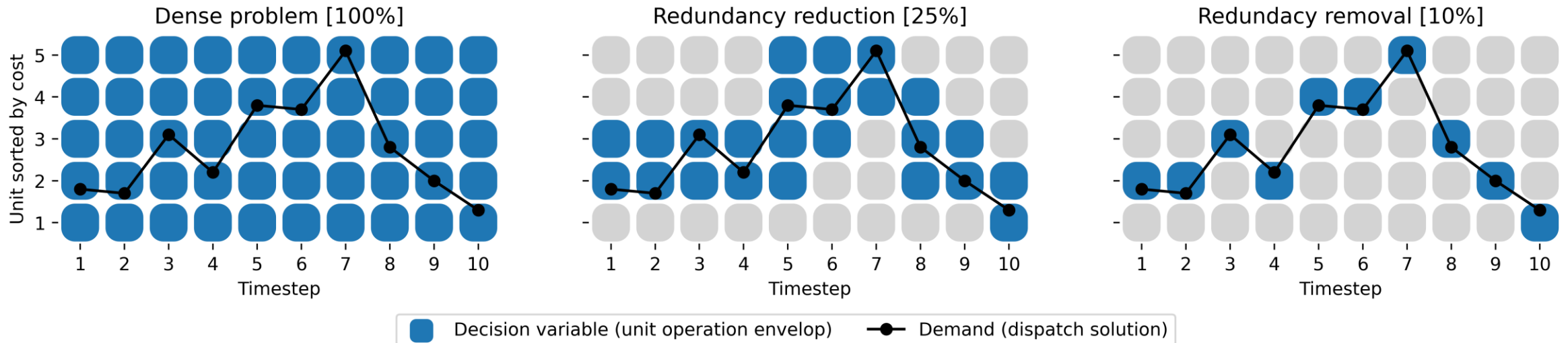
Is it possible to have error-free reduction?



[1] Zhi Gao, Matteo Gazzani, Diego A. Tejada-Arango, Abel Soares Siqueira, Ni Wang, Madeleine Gibescu, Germán Morales-España, Fully flexible temporal resolution for energy system optimization, Applied Energy, Volume 396, 2025, 126267, ISSN 0306-2619, <https://doi.org/10.1016/j.apenergy.2025.126267>.

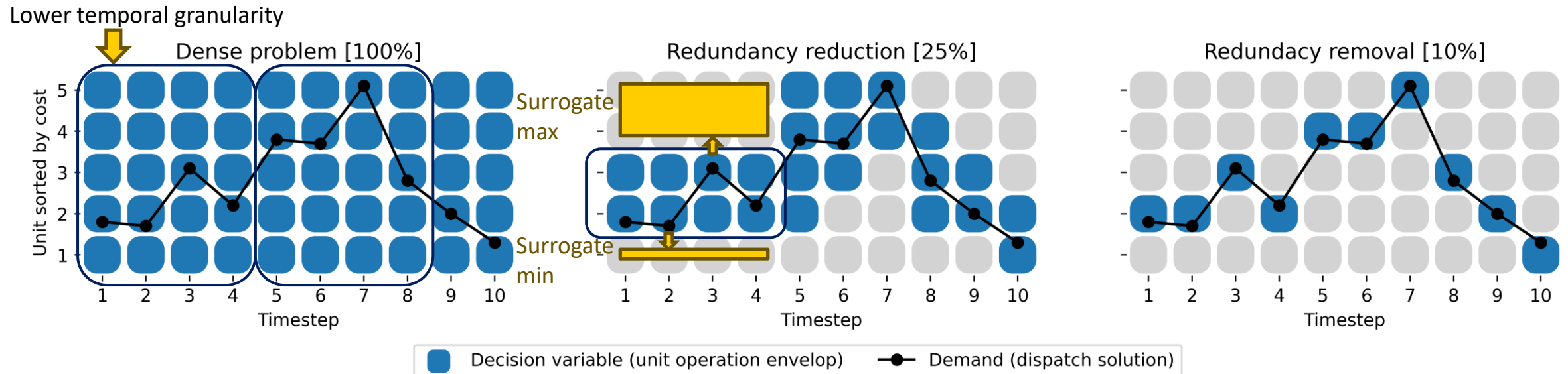
# Yes! If we can reduce “redundant” variables.

- Demonstration with a dispatch problem:  
5 production unit satisfying time-varying demand



# Yes! If we can reduce “redundant” variables.

- Demonstration with a dispatch problem:  
5 production unit satisfying time-varying demand
- Low-resolution surrogates examine the best/worst scenario in each window.  
Variables outside of the boundaries can therefore be removed error-free.
- Similar logic when we have variable availability (like VREnewables).



# Mathematical formulation

- Economic dispatch of national energy systems
- Surrogates are created in lower resolution, and min/max values of demand and capacity.

$$\begin{aligned}
 (P)(\mathbf{b}, \mathbf{e}, \mathcal{T}) : \min & \sum_{t \in \mathcal{T}} \sum_{u \in \mathcal{U}} \sum_{n \in \mathcal{N}(u)} \boxed{c_n x_{t,u,n}} && \text{Total production cost} && (1a) \\
 s.t. & \boxed{\sum_{n \in \mathcal{N}(u)} x_{t,u,n} = b_{t,u} \quad \forall t \in \mathcal{T}, u \in \mathcal{U}} && \text{Energy balance of country } u && (1b) \\
 & \boxed{x_{t,u,n} \leq e_{t,u,n} \quad \forall t \in \mathcal{T}, u \in \mathcal{U}, n \in \mathcal{N}(u)} && \text{Capacity constraint of generator } n && (1c)
 \end{aligned}$$

where  $x_{t,u,n}, e_{t,u,n}, c_n \in \mathbb{R}_{\geq 0}, b_{t,u} \in \mathbb{R}_{\geq 0} \quad \forall t \in \mathcal{T}.$



# Preservation of accuracy (error-free)

- Mathematical proof led by Maaïke Elgersma from TU Delft.



**Theorem 1.** Consider the LP  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$  as defined in (1). We also consider  $(\underline{P})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T})$  and  $(\bar{P})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T})$ , where

$$\bar{\mathbf{b}} \in [\mathbf{b}, \infty), \underline{\mathbf{b}} \in [0, \mathbf{b}], \bar{\mathbf{e}} \in [\mathbf{e}, \infty), \underline{\mathbf{e}} \in [0, \mathbf{e}]. \quad (4)$$

If  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$ ,  $(\underline{P})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T})$  and  $(\bar{P})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T})$  are feasible, and  $c_i \neq c_j \ \forall i, j \in \mathcal{N}$  where  $i \neq j$ , then for any optimal solutions  $\underline{\mathbf{x}}$  and  $\bar{\mathbf{x}}$  to  $(\underline{P})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T})$  and  $(\bar{P})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T})$ , respectively, any optimal solution  $\mathbf{x}^*$  to  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$  satisfies

$$\min(\underline{x}_{t,u,n}, e_{t,u,n}) \leq x_{t,u,n}^* \quad \forall t \in \mathcal{T}, u \in \mathcal{U}, n \in \mathcal{N}(u) \quad (5)$$

and

$$\bar{x}_{t,u,n} < \underline{e}_{t,u,n} \Rightarrow x_{t,u,n}^* \leq \bar{x}_{t,u,n} \quad \forall t \in \mathcal{T}, u \in \mathcal{U}, n \in \mathcal{N}(u). \quad (6)$$

*Proof.* Suppose  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$ ,  $(\underline{P})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T})$  and  $(\bar{P})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T})$  are feasible. Let  $\mathbf{x}^*$ ,  $\underline{\mathbf{x}}$ , and  $\bar{\mathbf{x}}$  be optimal solutions to these problems, respectively. We show that  $\mathbf{x}^*$  meets (5) and (6).

**There must be optimal solutions within the surrogate bounds**

**Corollary 1.** Consider LP  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$  as defined in (1) and the underestimation surrogate LP  $(\underline{S})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T}')$  as defined in (2) with any subset  $\mathcal{T}'$  of time steps  $\mathcal{T}$ , where

$$\underline{b}_{k,u} = \min_{t \in S_k} (b_{t,u}), \quad \bar{e}_{k,u,n} = \max_{t \in S_k} (e_{t,u,n}) \quad (10)$$

$\forall k \in \mathcal{T}', u \in \mathcal{U}, n \in \mathcal{N}(U)$ . Consider also the overestimation surrogate LP  $(\bar{S})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T}')$  as defined in (2), where

$$\bar{b}_{k,u} = \max_{t \in S_k} (b_{t,u}), \quad \underline{e}_{k,u,n} = \min_{t \in S_k} (e_{t,u,n}) \quad (11)$$

$\forall k \in \mathcal{T}', u \in \mathcal{U}, n \in \mathcal{N}(U)$ .

If  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$ ,  $(\underline{S})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T}')$ , and  $(\bar{S})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T}')$  are feasible, and  $c_i \neq c_j \ \forall i, j \in \mathcal{N}$  where  $i \neq j$ , then for any optimal solutions  $\underline{\mathbf{x}}$  and  $\bar{\mathbf{x}}$  to  $(\underline{S})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T}')$  and  $(\bar{S})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T}')$ , respectively, any optimal solution  $\mathbf{x}^*$  to  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$  satisfies

$$\min(\underline{x}_{k,u,n}, e_{t,u,n}) \leq x_{t,u,n}^* \quad (12)$$

$\forall k \in \mathcal{T}', t \in S_k, u \in \mathcal{U}, n \in \mathcal{N}(u)$  and

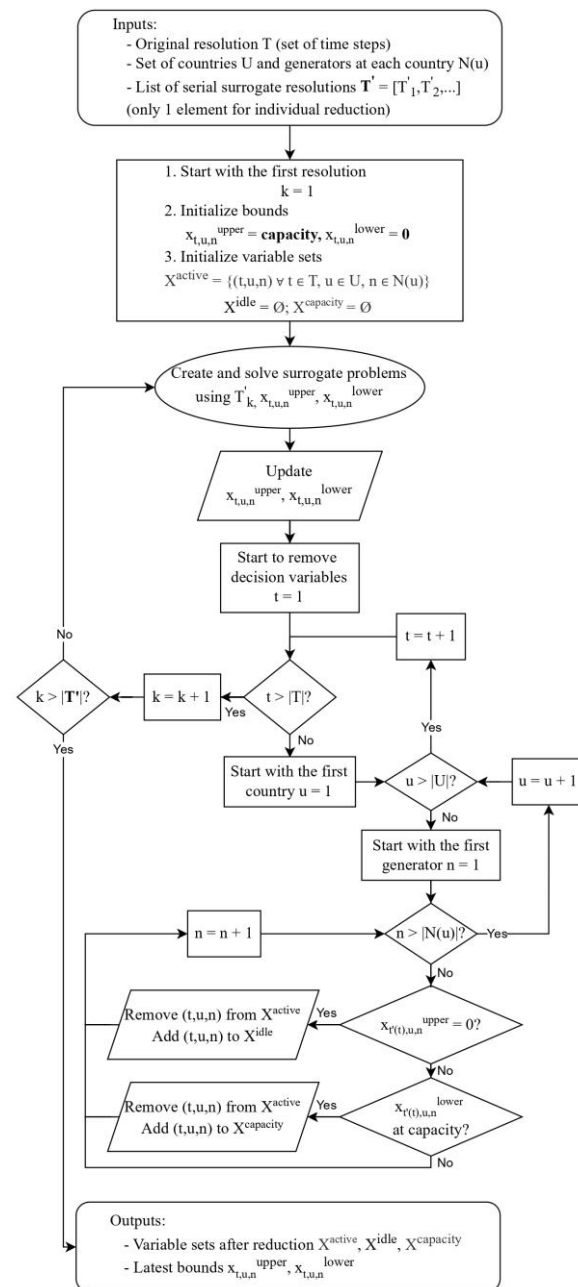
$$\bar{x}_{k,u,n} < \underline{e}_{k,u,n} \Rightarrow x_{t,u,n}^* \leq \bar{x}_{k,u,n}, \quad (13)$$

$\forall k \in \mathcal{T}', t \in S_k, u \in \mathcal{U}, n \in \mathcal{N}(u)$ .

*Proof.* Suppose  $(P)(\mathbf{b}, \mathbf{e}, \mathcal{T})$ ,  $(\underline{S})(\underline{\mathbf{b}}, \bar{\mathbf{e}}, \mathcal{T}')$ , and  $(\bar{S})(\bar{\mathbf{b}}, \underline{\mathbf{e}}, \mathcal{T}')$  are feasible. We first show that any optimal solutions to

**Low-resolution surrogates can be used for this.**

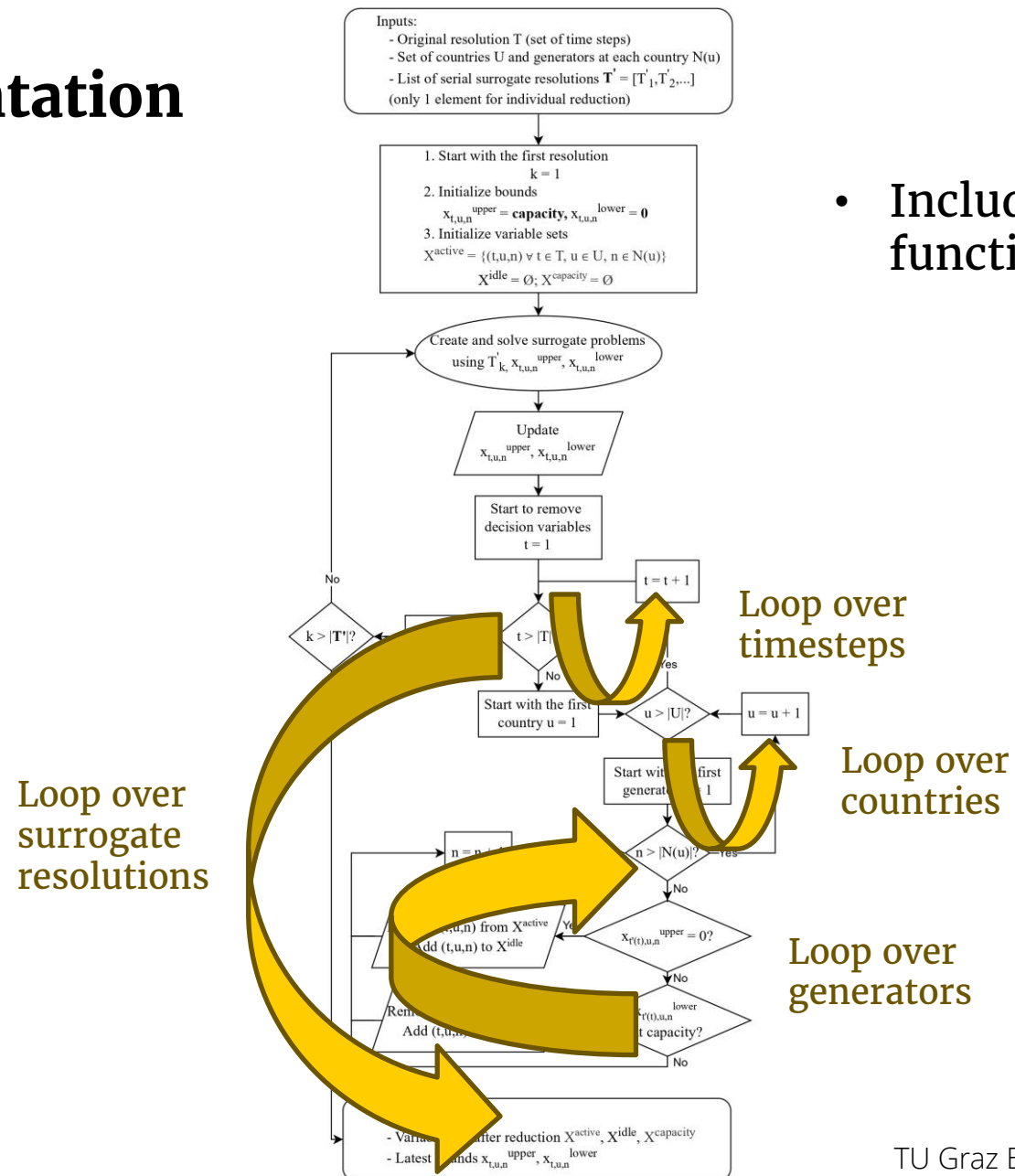
# Implementation



- Including individual & serial surrogate functions.

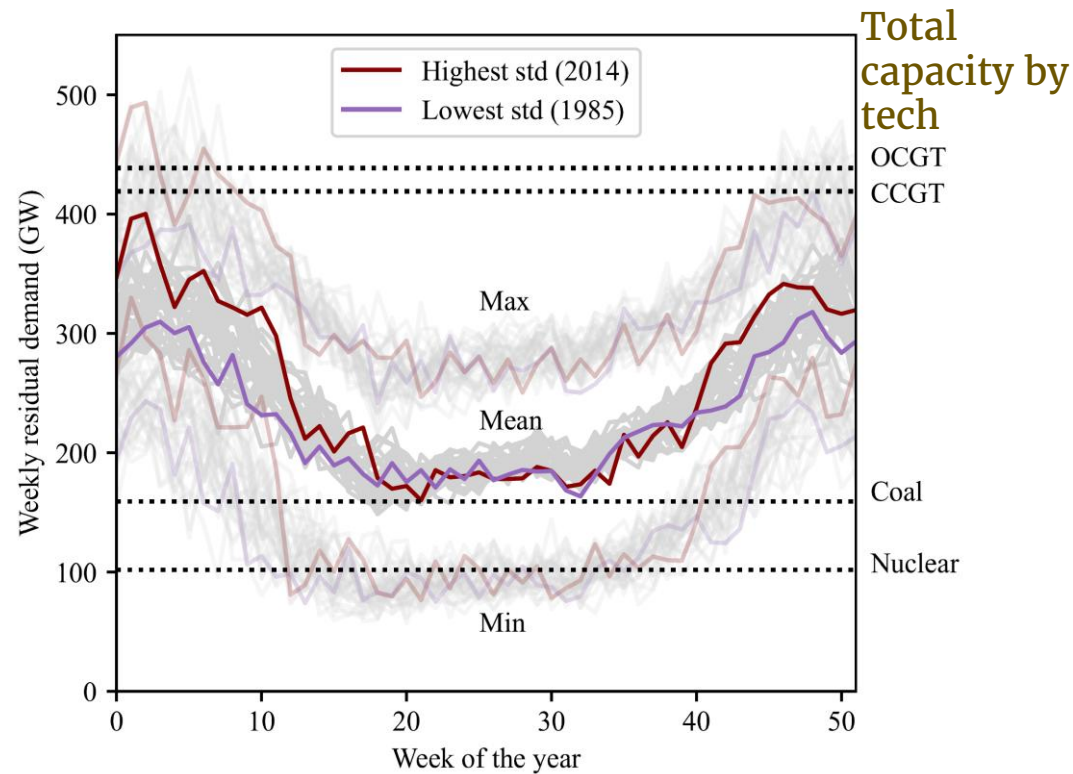
# Implementation

- Including individual & serial surrogate functions.



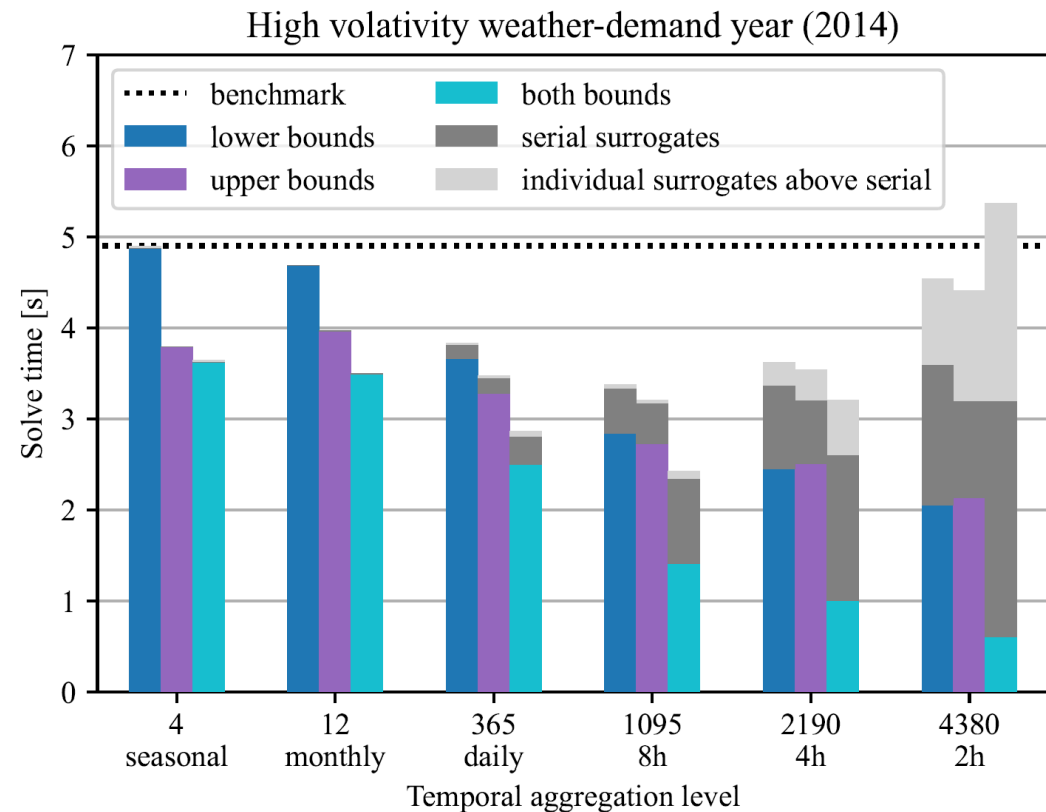
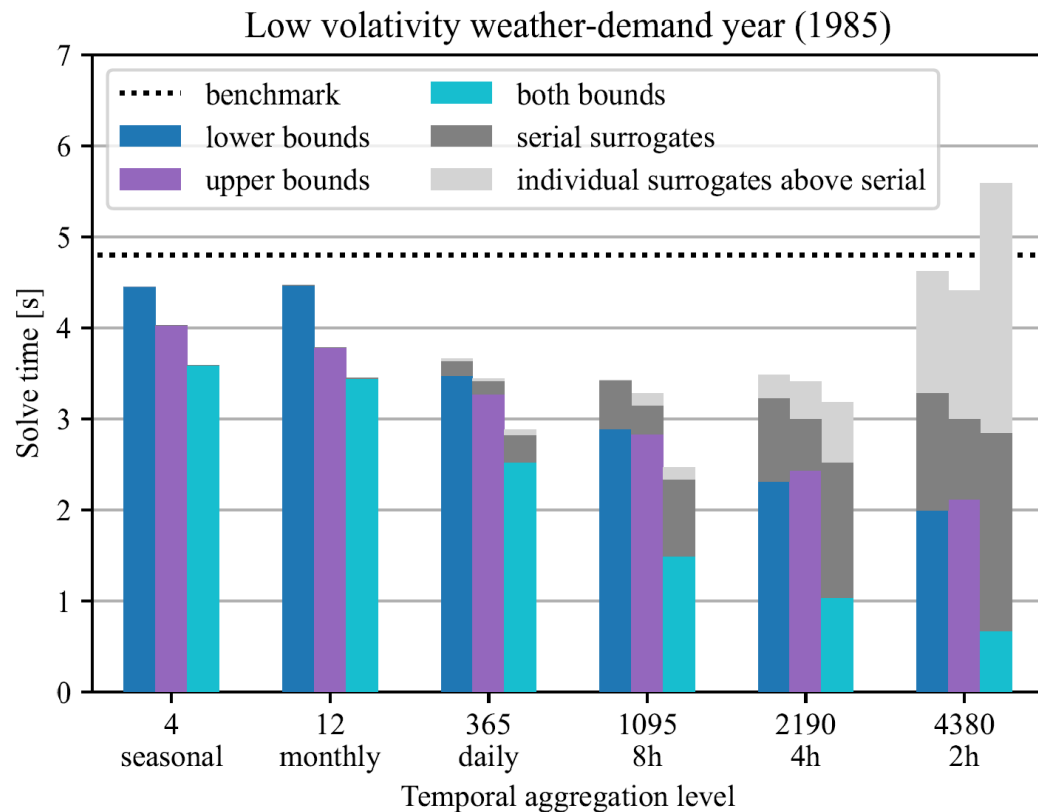
## Case study (based on TYNDP 24)

- Economic dispatch of 35 national energy systems.
- Under the most stable and most fluctuating demand-weather years.
- Note: there is no energy storage, no transmission lines.



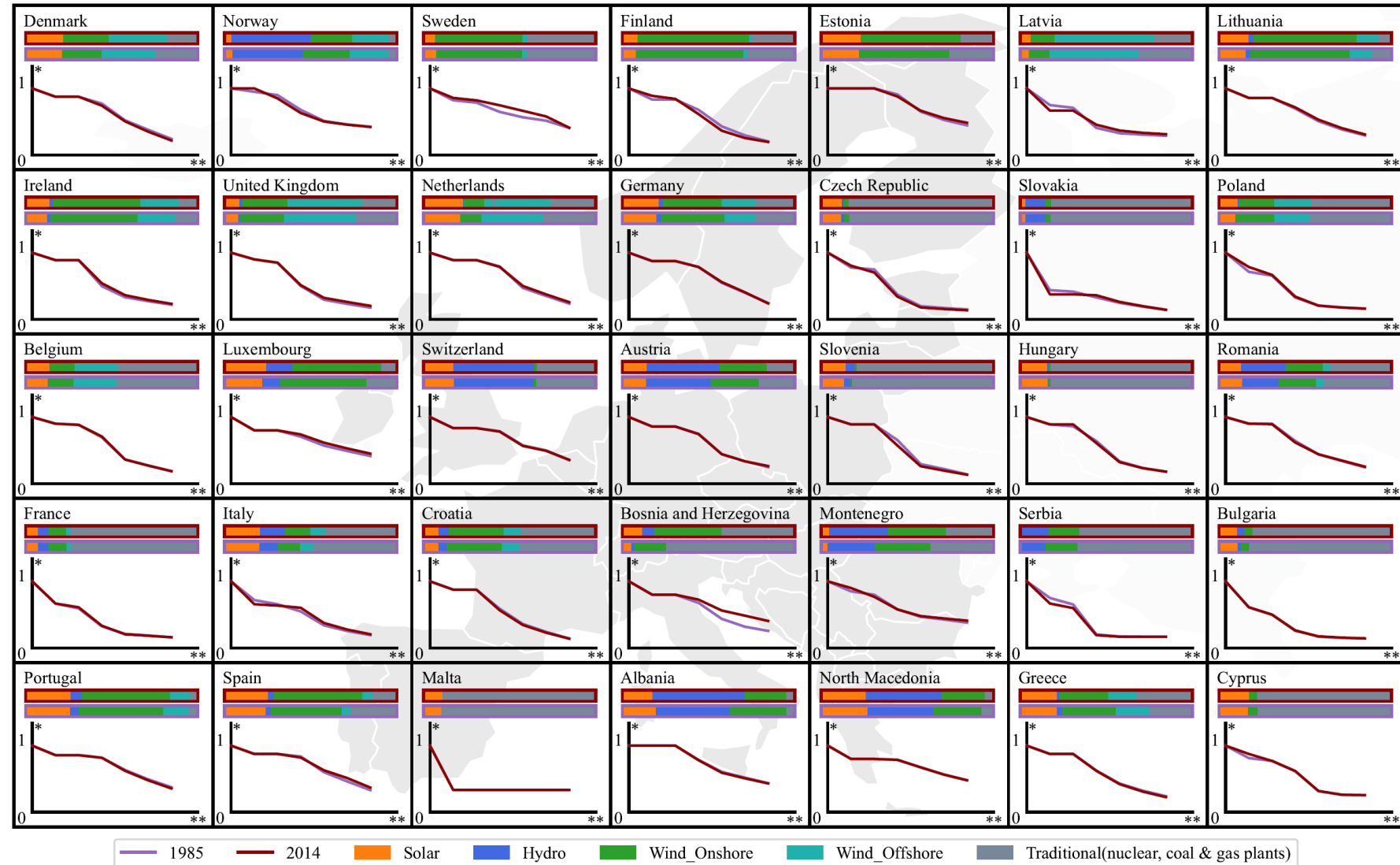
# Case study (based on TYNDP 24)

- Significant gains in computational efficiency
- And memory usage (next slide)
- Note again: all instances error-free



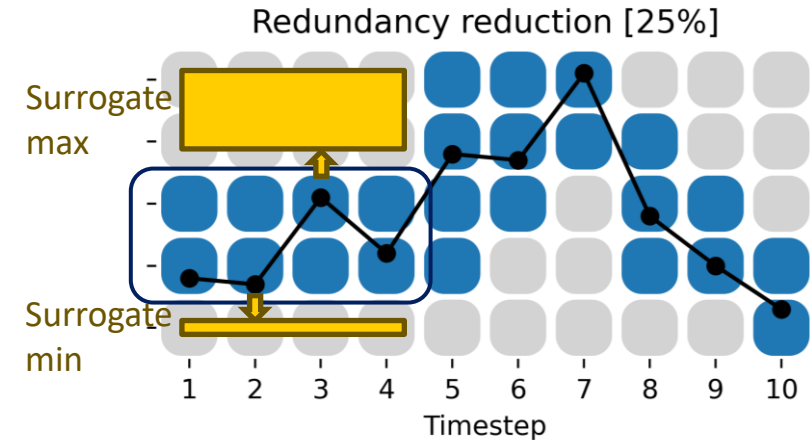
# Reduction of decision variables

- Country-country comparison  
(Estonia & Czech top)  
(Spain & Malta below)
- Climate year comparison  
(Bosnia and Herzegovina)



# Overcoming the efficiency-accuracy trade-off

- There are “free lunches”, big lunches
- Why this is ground-breaking
- How, in short
- More on the way
  - Extend to include more system features (storage, network etc.).
  - Re-think the use of computing power.



Let's keep in touch (Zhi will be open for PostDoc opportunities ☺)

Zhi Gao, Maaike Elgersma, Madeleine Gibescu, Germán Morales-España, Mathijs de Weerd, Matteo Gazzani,  
Error-free model reduction with low-resolution precursor surrogates for energy system optimization.  
[submitted to PSCC 26]



**Utrecht  
University**

Sharing science,  
*shaping tomorrow*